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**Supplementary information**

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**Superconductivity in pressurized trilayer  
 $\text{La}_4\text{Ni}_3\text{O}_{10-\delta}$  single crystals**

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## Supplementary Information for

### Superconductivity in pressurized trilayer $\text{La}_4\text{Ni}_3\text{O}_{10-\delta}$ single crystals

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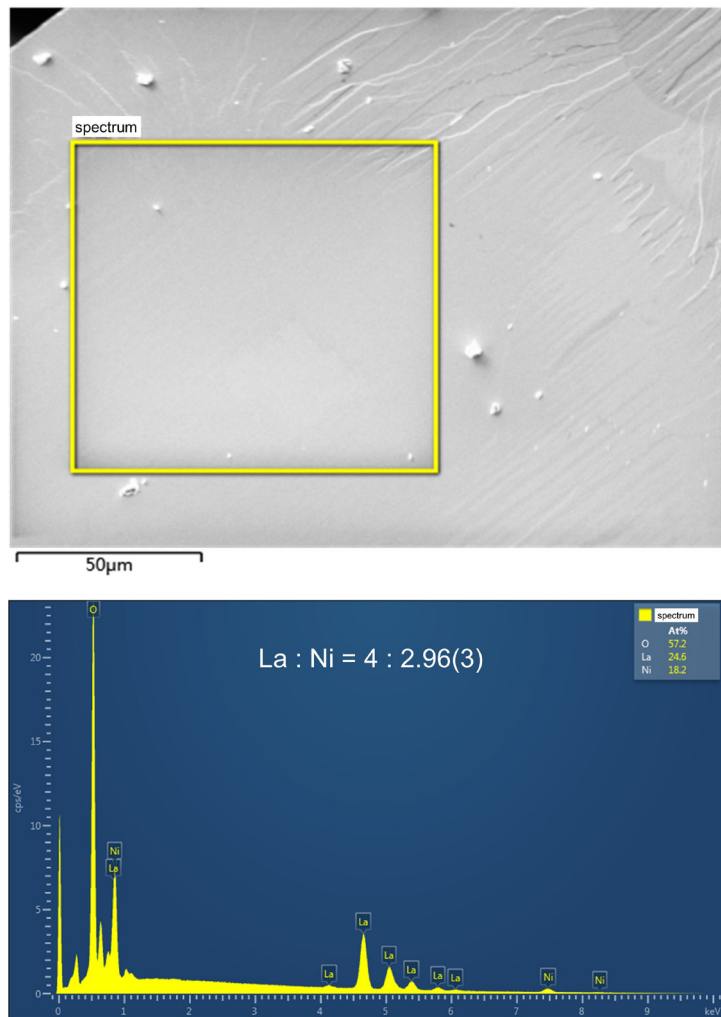
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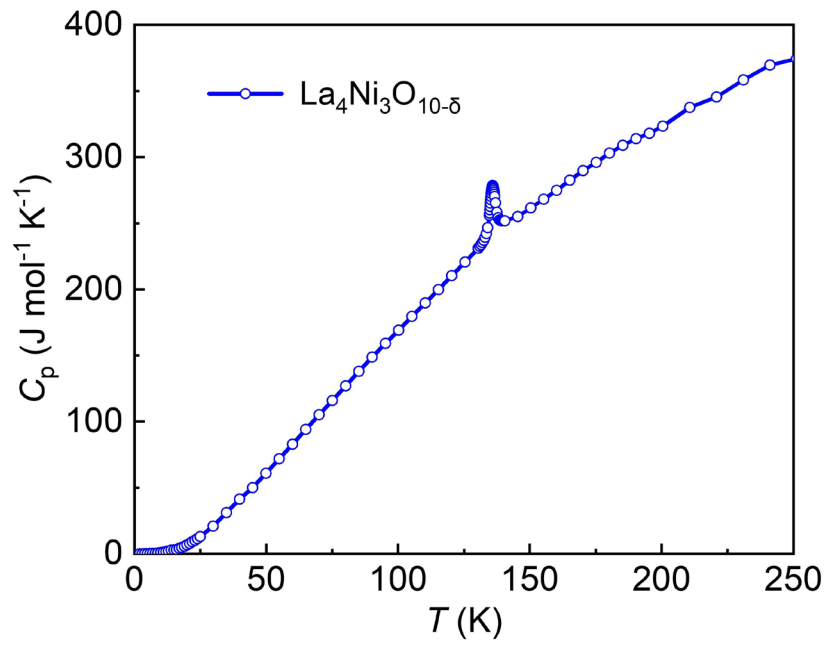
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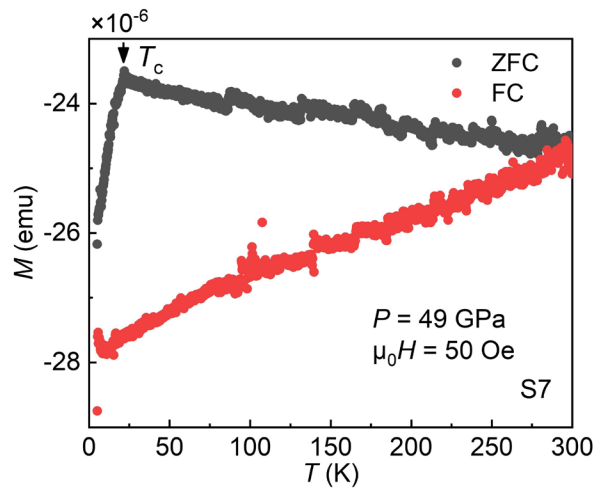
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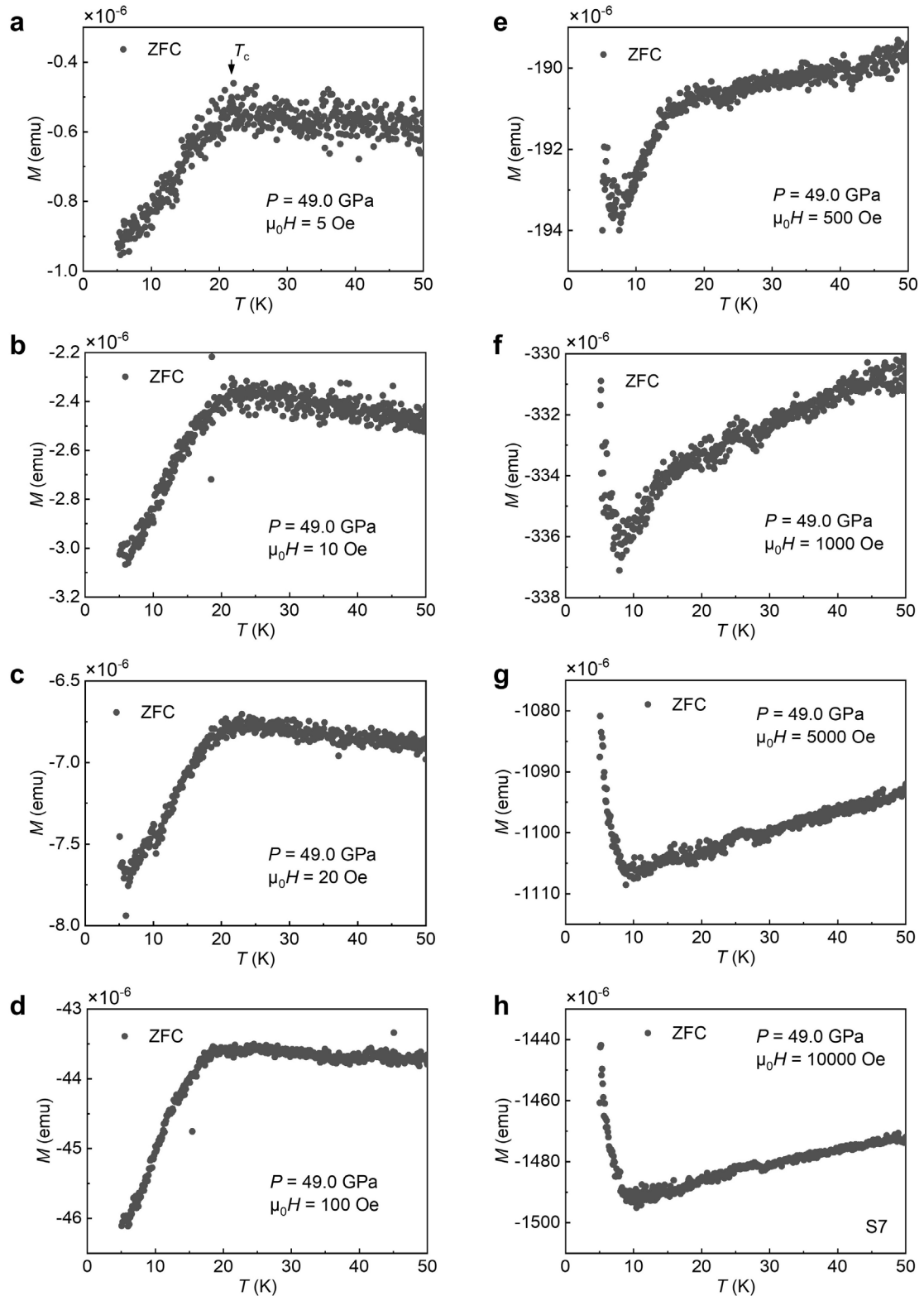
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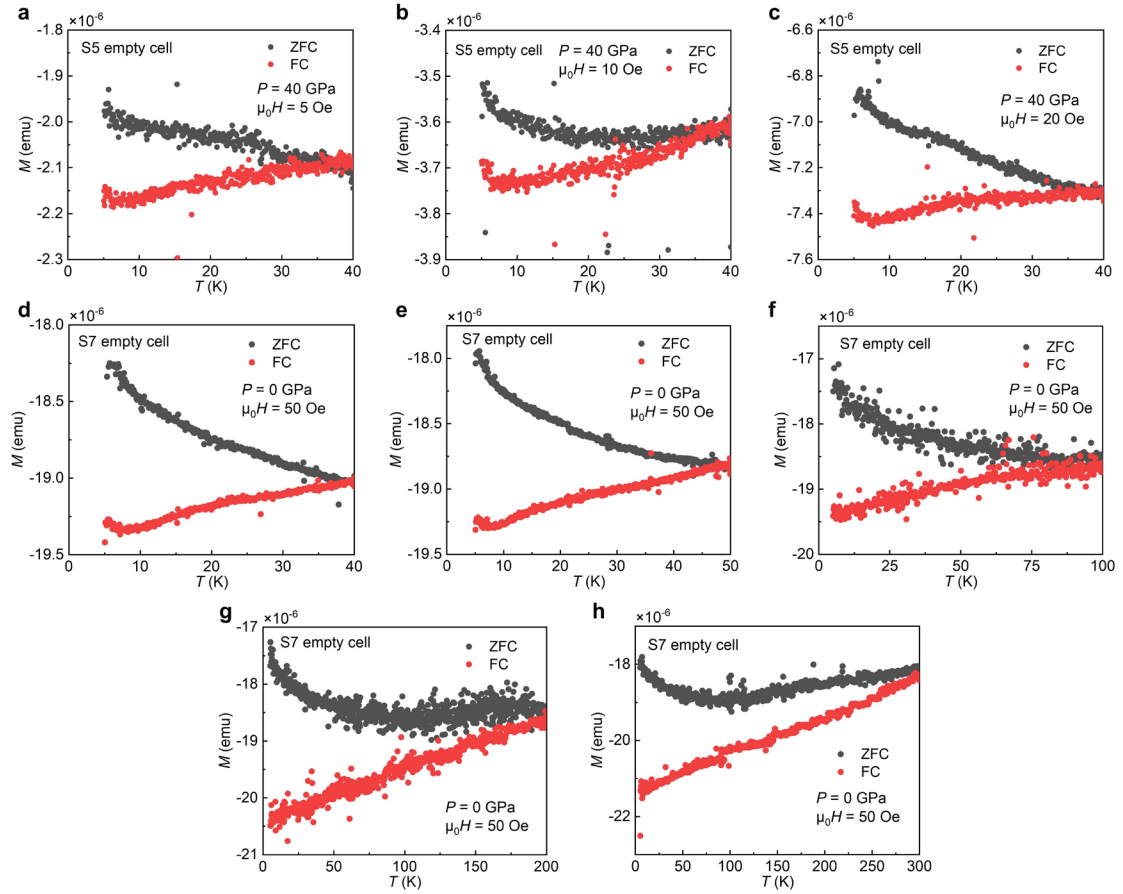
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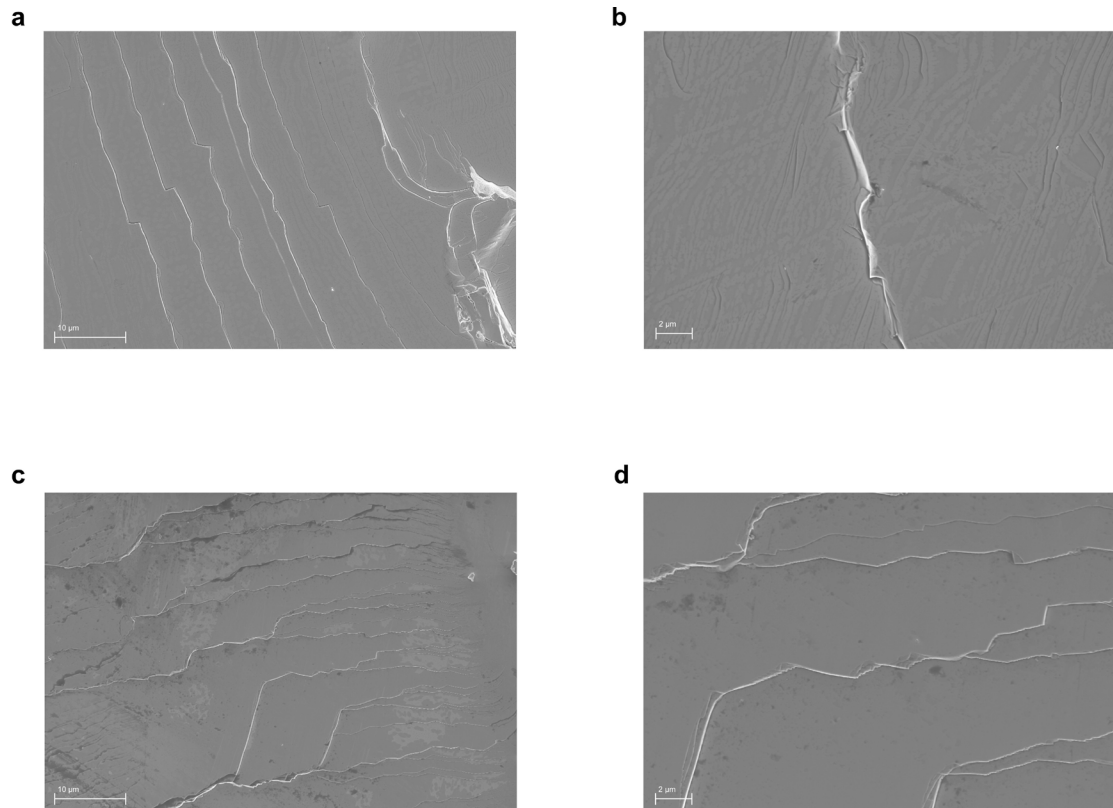
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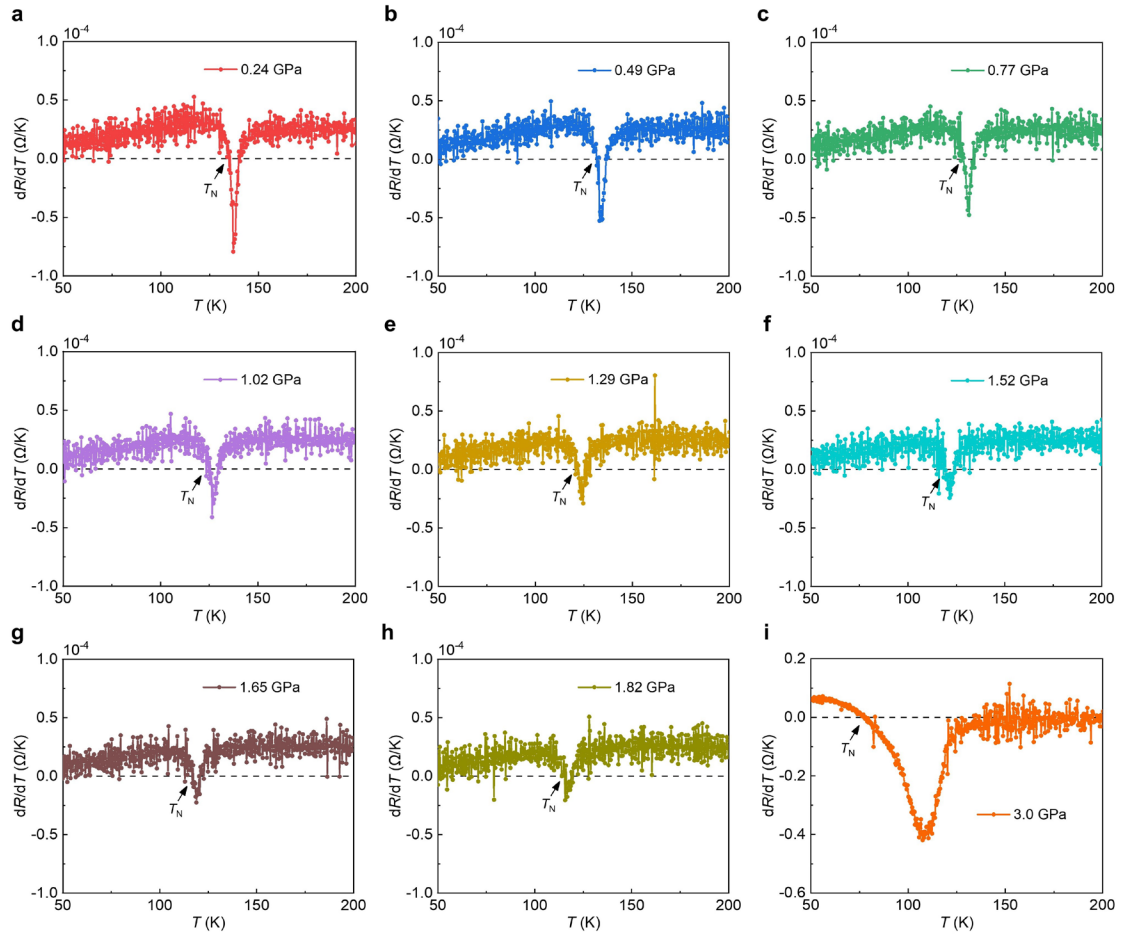
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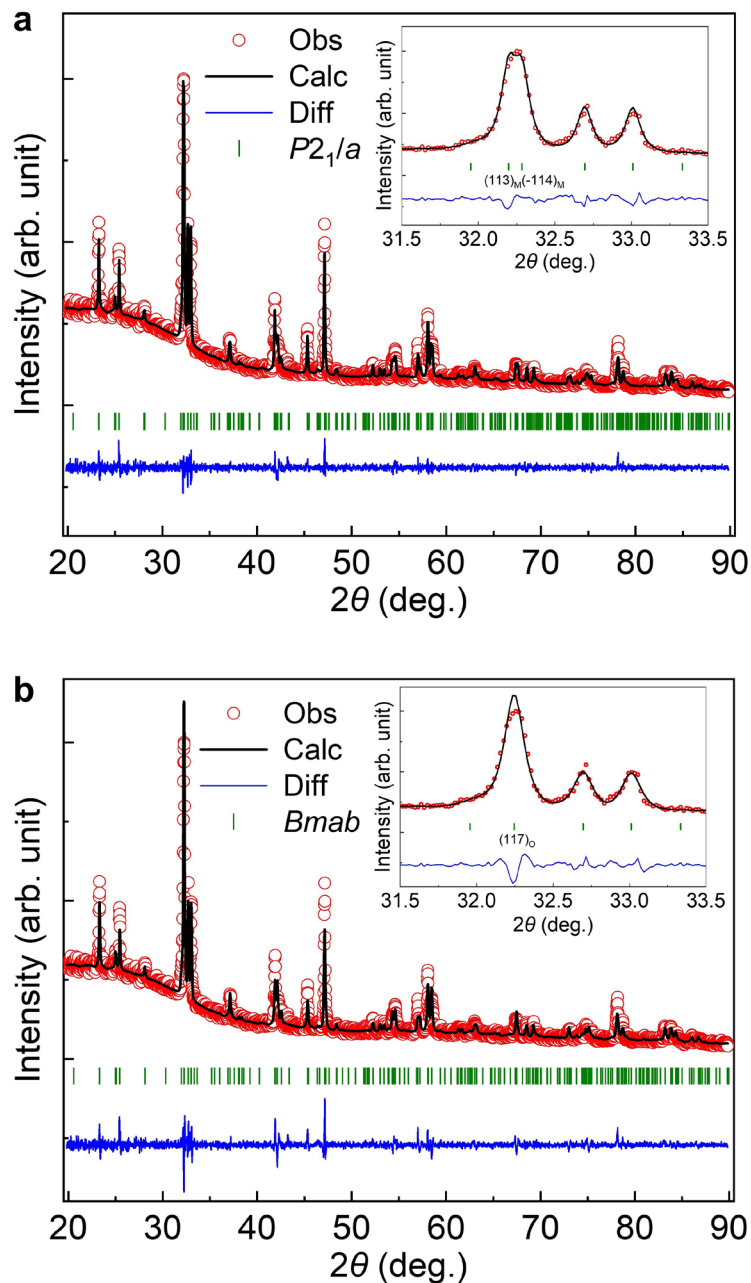
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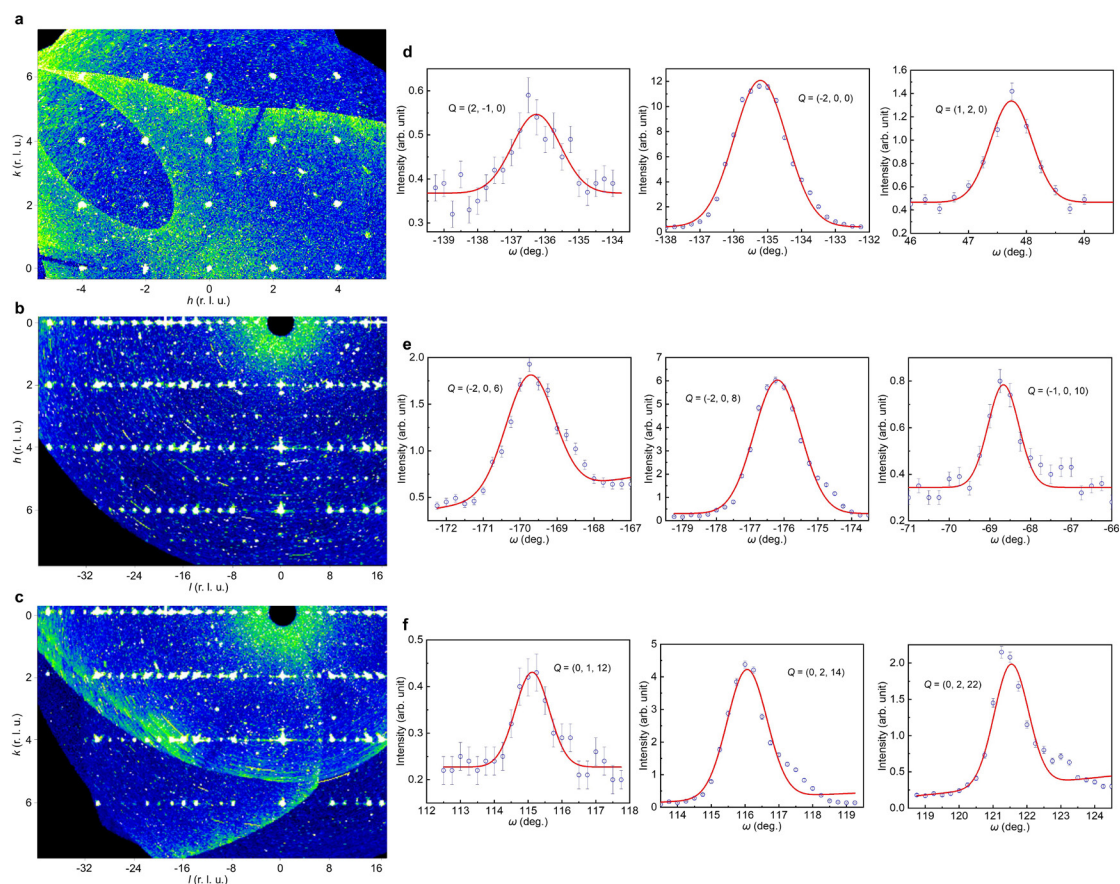
**Supplementary Fig. 6** | The surface morphology of the cleavage plane of La<sub>4</sub>Ni<sub>3</sub>O<sub>10-δ</sub> single crystals observed through scanning electron microscopy (SEM). SEM images **a**, and **c**, were obtained with a scale bar of 10 μm. Zoom-in SEM images **b**, and **d**, were obtained with a scale bar of 2 μm. Across all images, no detectable impurities were found, affirming the purity of the single crystals utilized in high-pressure resistance and susceptibility measurements.



**Supplementary Fig. 7** | The derivatives of the temperature-dependent resistance curves ( $dR/dT$ ) derived from Figs. 3a and 3b under varying pressures. **a**, 0.24 GPa; **b**, 0.49 GPa; **c**, 0.77 GPa; **d**, 1.02 GPa; **e**, 1.29 GPa; **f**, 1.52 GPa. **g**, 1.65 GPa. **h**, 1.82 GPa. **i**, 3.0 GPa. The Néel temperature ( $T_N$ ) from resistivity measurements is identified at the maximum of the resistance anomaly, where the temperature derivative  $dR/dT$  equals zero. Resistance anomalies at 11 GPa and 15.5 GPa in Fig. 3b, which are influenced by the onset of superconductivity, complicate accurate estimation of  $T_N$  and therefore are not included.



**Supplementary Fig. 8** | Comparison of  $P2_1/a$  and  $Bmab$  structural models at ambient condition. **a**, Rietveld refinement of a lab-based XRD pattern for powdered  $\text{La}_4\text{Ni}_3\text{O}_{10-\delta}$  single crystals at ambient pressure and room temperature. Black solid lines represent the fit to the experimental data, shown by red circles. Blue solid lines indicate the residual difference between observed and calculated intensities. Short vertical green bars mark the positions of expected Bragg peaks. This dataset fits well with the  $P2_1/a$  space group (GOF = 2.0,  $R_p$  = 4.12,  $R_{wp}$  = 5.46). The inset shows the details near  $32.2^\circ$ , where the  $(1\ 1\ 3)_M$  and  $(-1\ 1\ 4)_M$  peaks are captured by the  $P2_1/a$  model. **b**, Rietveld refinement for the  $Bmab$  structure using the same XRD data (GOF = 2.4,  $R_p$  = 4.74,  $R_{wp}$  = 6.62). The inset shows that the  $Bmab$  model fails to resolve the double peak structure near  $32.2^\circ$ , instead presenting a single peak of  $(1\ 1\ 7)_O$  which suggests a less accurate representation of the underlying crystal structure. The measurements were carried out on a Bruker D8 Discover diffractometer, utilizing Cu  $K\alpha$  radiation ( $\lambda=1.5406\ \text{\AA}$ ).



**Supplementary Fig. 9** | Single-crystal X-ray and neutron diffraction measurements of  $\text{La}_4\text{Ni}_3\text{O}_{10-\delta}$  at ambient pressure and room temperature. For clarity in visualizing the main Bragg peaks corresponding to both the  $P2_1/a$  and  $Bmab$  structures, we have plotted the data based on the  $P2_1/a$  structure with  $Z=4$ , having unit cell dimensions  $a = 5.4164 \text{ \AA}$ ,  $b = 5.4623 \text{ \AA}$ , and  $c = 27.985 \text{ \AA}$ . **a**,  $(hk)$  reciprocal plane reconstructed from X-ray diffraction measurements. In addition to the strong Bragg peaks corresponding to the  $Bmab$  structure, which occur when both  $h$  and  $k$  are even, additional weaker peaks (when  $h$   $k$  are integers) due to the monoclinic distortion inherent to the  $P2_1/a$  structure are also observed. This indicates  $Bmab$  space group cannot accurately represent the structure; **b**,  $(h0l)$  reconstructed reciprocal plane; **c**,  $(0kl)$  reconstructed reciprocal plane; **d**, Representative neutron diffraction rocking curves of the  $(hk0)$  Bragg peaks; **e**,  $(h0l)$  Bragg peaks; **f**,  $(0kl)$  Bragg peaks. The comparisons between the measured and calculated intensities of these Bragg peaks can be found in Extended Data Fig. 7a. The X-ray diffraction measurements were conducted using a lab-based Bruker D8 Venture diffractometer, while the neutron diffraction measurements utilized the HB-3A four-circle single-crystal neutron diffractometer. Error bars, 1 s.d.

**Supplementary Table 1** Crystallographic parameters derived from a combined single-crystal refinement of neutron and X-ray diffractions on La<sub>4</sub>Ni<sub>3</sub>O<sub>9.96</sub> single crystals, at ambient pressure and room temperature. All O occupancies are constrained between 0 and 1.

<i>P2<sub>1</sub>/a (Z = 2)</i>				
<i>a</i> = 5.4164(3) Å		<i>b</i> = 5.4623(3) Å		<i>c</i> = 14.2279(2) Å
<i>α</i> = 90°		<i>β</i> = 100.75°		<i>γ</i> = 90°
<b>Atomic positions</b>				
<b>Name (site)</b>	<b><i>x</i></b>	<b><i>y</i></b>	<b><i>z</i></b>	<b><i>Occ</i></b>
La1 (4e)	0.803(1)	0.508(1)	0.103(1)	1.00
La2 (4e)	0.939(1)	0.500(1)	0.364(1)	1.00
Ni1 (2d)	0.5	0.5	0.5	1.00
Ni2 (4e)	0.862(1)	0.002(1)	0.222(1)	1.00
O1 (4e)	0.786(5)	0.967 (2)	0.068(1)	1.00
O2 (4e)	0.066(4)	0.954(2)	0.636(1)	1.00
O3 (4e)	0.112(4)	0.742(5)	0.231(1)	1.00
O4 (4e)	0.113(4)	0.248(6)	0.211(1)	0.98(2)
O5 (4e)	0.771(4)	0.723(4)	0.486(1)	1.00

R<sub>F</sub> = 2.99, R<sub>F2</sub> = 4.10, R<sub>wF2</sub> = 7.32

**Supplementary Table 2** Crystallographic parameters obtained from the single-crystal refinement of XRD data in  $\text{La}_4\text{Ni}_3\text{O}_{10-\delta}$ , conducted at 19.5 GPa and room temperature. A methanol-ethanol-water mixture in the ratio of 16:3:1 was used as the pressure-transmitting medium for the measurement.

<i>I4/mmm (Z = 2)</i>			
$a = 3.73(1) \text{ \AA}$	$b = 3.73(1) \text{ \AA}$	$c = 27.2(1) \text{ \AA}$	
$\alpha = 90^\circ$	$\beta = 90^\circ$	$\gamma = 90^\circ$	
<b>Atomic positions</b>			
<b>Name (site)</b>	<b>x</b>	<b>y</b>	<b>z</b>
La1 (4e)	1.0	1.0	0.432(1)
La2 (4e)	1.0	1.0	0.302(1)
Ni1 (2a)	0.5	0.5	0.5
Ni2 (4e)	0.5	0.5	0.358(1)
O1 (8g)	1	0.5	0.363(1)
O2 (4e)	0.5	0.5	0.392(8)
O3 (4c)	0	0.5	0.5
O4 (4e)	0.5	0.5	0.281(2)

$R_F = 6.25$ ,  $R_{F2} = 9.28$ ,  $R_{wF2} = 14.8$

**Supplementary Table 3** Crystallographic parameters of pressurized  $\text{La}_4\text{Ni}_3\text{O}_{10-\delta}$  obtained from Rietveld refinements of high-pressure synchrotron XRD. Helium was used as the pressure-transmitting medium for the measurement.

Pressure (GPa)	a(Å)	b(Å)	c(Å)	$\beta$ (°)	GOF	$R_p$ (%)	$R_{wp}$ (%)	Space group
0	5.4142(4)	5.4647(4)	14.220(1)	100.66	0.99	5.66	6.88	$P2_1/a$
2.5	5.3852(3)	5.4321(3)	14.147(1)	100.71	0.72	8.03	7.11	$P2_1/a$
3.5	5.3769(40)	5.4111(39)	14.127(12)	100.67	0.22	9.69	9.30	$P2_1/a$
5.0	5.3675(8)	5.3962(8)	14.100(3)	100.75	0.79	9.19	7.86	$P2_1/a$
6.5	5.3478(4)	5.3824(4)	14.085(1)	100.80	1.2	10.9	10.4	$P2_1/a$
8.3	5.3320(6)	5.3522(8)	13.983(2)	100.67	1.0	8.68	8.63	$P2_1/a$
10.0	5.3250(5)	5.3406(5)	13.972(1)	100.76	0.93	10.4	8.91	$P2_1/a$
11.7	5.2950(4)	5.3265(5)	13.910(1)	100.66	0.72	8.00	6.91	$P2_1/a$
13.7	3.7485(6)	3.7485(6)	27.346(5)	90	1.0	7.15	7.55	$I4/mmm$
15.2	3.7310(1)	3.7310(1)	27.207(1)	90	0.88	7.13	6.91	$I4/mmm$
17.2	3.7245(1)	3.7245(1)	27.130(1)	90	0.85	7.46	7.19	$I4/mmm$
18.7	3.7177(6)	3.7177(6)	27.053(5)	90	0.72	7.13	6.53	$I4/mmm$
21.6	3.7121(1)	3.7121(1)	27.023(2)	90	0.61	6.50	5.86	$I4/mmm$
24.0	3.6934(1)	3.6934(1)	26.880(1)	90	0.78	5.92	5.94	$I4/mmm$
27.1	3.6879(1)	3.6879(1)	26.854(2)	90	0.75	7.15	6.92	$I4/mmm$
30.0	3.6716(1)	3.6716(1)	26.704(2)	90	0.86	7.82	7.90	$I4/mmm$
34.0	3.6602(1)	3.6602(1)	26.609(2)	90	0.68	7.00	6.44	$I4/mmm$
38.0	3.6487(2)	3.6487(1)	26.534(2)	90	1.3	9.1	8.9	$I4/mmm$
42.0	3.6319(1)	3.6319(1)	26.452(2)	90	1.1	8.99	8.75	$I4/mmm$
48.0	3.6169(1)	3.6169(1)	26.316(1)	90	0.94	8.14	7.97	$I4/mmm$
52.0	3.6068(1)	3.6068(1)	26.243(1)	90	0.88	7.82	7.51	$I4/mmm$
56.0	3.5957(1)	3.5957(1)	26.186(2)	90	0.95	6.62	6.83	$I4/mmm$